

# Security-Performance Trade-off in DAG-based Proof-of-Work Blockchain Protocols

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In 585 papers presented at top CS conferences from 2020 to 2022



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- ▶ 41 papers focus on PoW:
  - - Formal Analysis of Nakamoto Consensus (10)
  - - New Design: DAG-based Protocols (7)
  - - New Design: non-DAG-based Protocols (6)
  - - Mining Attacks and Ecosystem Analysis (18)

➤ 23 papers involve PoS:

- - Analysis (11)
- - New Design (12)



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#### To sum up:

- Security Analysis
  - PoW: more secure than previously believed
  - PoS: more attack vectors discovered
- New PoS Designs: not sure we can ever achieve PoW's security
- PoS ecosystems: lack of studies raises concerns



➡ Nakamoto Consensus and its limitation

#### The solution: DAG-based blockchain

➡ Does DAG solve the problem?



The phenomena in DAG blockchain



■ NC (Bitcoin and its variants)

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Hash(pointer, tx, nonce) < Target change



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NC (Bitcoin and its varients)

- ledger: a chain of blocks
- participants: miners
  - generate block: Proof-of-Work

Hash(pointer, tx, nonce) < Target change

• extend chain: Longest-Chain rule

• the longest fork means the most mining power



orphaned

#### Limitations of NC



Security-Performance Tradeoff

#### Limitations of NC

#### Security-Performance Tradeoff

➤ security of NC is rooted in

"block generation interval >> the time for propagation"

• the smaller the gap, the worse the security



J. A. Garay, A. Kiayias, and N. Leonardos, "The bitcoin backbone protocol: Analysis and applications," in Advances in Cryptology -EUROCRYPT 2015 - 34th Annual International Conference on the Theory and Applications of Cryptographic Techniques, ser. Lecture Notes in Computer Science, vol. 9057. Springer, 2015, pp. 281–310.

—, "The bitcoin backbone protocol with chains of variable difficulty," in Advances in Cryptology - CRYPTO 2017 - 37th Annual International Cryptology Conference, ser. Lecture Notes in Computer Science, vol. 10401. Springer, 2017, pp. 291–323.

P. Gaži, A. Kiayias, and A. Russell, "Tight consistency bounds for bitcoin," in *Proceedings of the 2020 ACM SIGSAC Conference on Computer and Communications Security*, ser. CCS '20. ACM, 2020, p. 819–838. R. Pass, L. Seeman, and A. Shelat, "Analysis of the blockchain protocol in asynchronous networks," in Advances in Cryptology - EUROCRYPT 2017 - 36th Annual International Conference on the Theory and Applications of Cryptographic Techniques, ser. Lecture Notes in Computer Science, vol. 10211, 2017, pp. 643–673.

A. Dembo, S. Kannan, E. N. Tas, D. Tse, P. Viswanath, X. Wang, and O. Zeitouni, "Everything is a race and Nakamoto always wins," in CCS '20: 2020 ACM SIGSAC Conference on Computer and Communications Security. ACM, 2020, pp. 859–878.

L. Kiffer, R. Rajaraman, and A. Shelat, "A better method to analyze blockchain consistency," in *Proceedings of the 2018 ACM SIGSAC Conference on Computer and Communications Security, CCS 2018*, pp. 729–744.



## Limitations of NC

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Y. Sompolinsky and A. Zohar, "Secure high-rate transaction processing in Bitcoin," in *Financial Cryptography and Data Security - 19th International Conference, FC 2015*, ser. Lecture Notes in Computer Science, vol. 8975. Springer, 2015, pp. 507–527.

J. A. Garay, A. Kiayias, and N. Leonardos, "The bitcoin backbone protocol: Analysis and applications," in Advances in Cryptology -EUROCRYPT 2015 - 34th Annual International Conference on the Theory and Applications of Cryptographic Techniques, ser. Lecture Notes in Computer Science, vol. 9057. Springer, 2015, pp. 281–310.

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#### > however!

higher throughput requires larger block and shorter block interval, which reduces the security

NC has to maintain a poor performance.
 > 7 TPS





■ Structure: Chain → Directed Acyclic Graph



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- > multiple predecessors
- > multiple concurrent blocks



A large number of valid blocks result in a high throughput (thousands TPS)

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- Security is a concern for early protocols
  > weak security guarantees
   Inclusive, Meshcash
  > partial security analyses
  - SPECTRE, PHANTOM, Conflux

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State-of-the-art:

Prism (CCS' 2019), OHIE (S&P 2020)





Structured DAG blockchain based on NC

#### Prism & OHIE



Structured DAG blockchain based on NC
 Prism [CCS'19] (three types of blocks)

• tx blocks, proposer blocks, voter blocks



V. K. Bagaria, S. Kannan, D. Tse, G. Fanti, and P. Viswanath, "Prism: Deconstructing the blockchain to approach physical limits," in *Proceedings of the 2019 ACM SIGSAC Conference on Computer and Communications Security, CCS 2019.* ACM, 2019, pp. 585–602.

#### Prism & OHIE



Structured DAG blockchain based on NC
 Prism [CCS'19] (three types of blocks)

• tx blocks, proposer blocks, voter blocks

#### OHIE [S&P'20] (multiple parallel chains)

- m parallel NC chains, m times throughput
- security comparable to NC



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Security-Performance tradeoff has been broken

- ▶ Prism and OHIE achieve 90% and 50% bandwidth utilization
- > Both designs prove the same security properties as NC



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Security-Performance tradeoff really has been broken?

#### Assumption of Decoupling

- some priority blocks are small enough and enjoy a priority propagation policy
  - delay is always very small
  - always accept immediately



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  - always accept immediately
- Security will be guaranteed if these priority blocks can always be "synchronized quickly"
- > But it's not easy in a high-throughput DAG-based blockchain system

#### Block Jam



If the total number of blocks propagated over a period of time exceeds the network's processing capacity, some blocks will have more propagation delay





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#### In DAG-based blockchain system

- many blocks generated parallelly
- network loads many blocks→block propagation delay vary and increases



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R. Zhang, D. Zhang, Q. Wang, S. Wu, J. Xie, and B. Preneel, "NC-Max: Breaking the security-performance tradeoff in Nakamoto consensus," *The Network and Distributed System Security (NDSS) Symposium*, 2022.





## 1. NC & DAG 2. New Model

3. LP Attack

4. Examples & Simulation



→ Why we need a new model?

Characteristics of CBM







For DAG-based blockchain

multiple types of blocks

> overlaps in block propagation

 $\rightarrow$  delay is complex and diverse



#### For DAG-based blockchain

multiple types of blocks

Inductive types of blocks
 Overlaps in block propagation
 delay is complex and diverse

#### UDBM

- ➤ a uniform upper bound of delay on all blocks
- > adversary strategy: delay all receivers to the bound

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#### UDBM

- > a uniform upper bound of delay on all blocks
- > adversary strategy: delay all receivers to the bound

- We deploy Prism with SimBlock
  - > a maximum delay bound would overestimate the security requirement



\*actual delay is the interval between the block's generation

and the arrival of its latest predecessor at a certain node



Delay of proposer blocks

delay is complex and diverse


**CBM** 



#### CBM

- > time assumption
  - the upper bound may be different
  - specify delay of each node



# V PARA



- > time assumption
  - the upper bound may be different
  - specify delay of each node

## block processing: distinguish the status

• received, accepted, confirmed, orphaned

actual delay = propagation delay + processing delay

same adversary & mining & security property



propagation delay

actual delay



Defining late-predecessors (LP)

- >  $B^*$  is late if  $B^* \leftarrow B^+$ , but  $B^+$  is received first
- > interval between receiving  $B^*$  and  $B^+$  is lag time



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- late received time accepted time

- Bounding the Actual Delay
  - ➤ max actual delay =

propagation delay (itself) + max lag time (predecessors)  $\leq$  max propagation delay (predecessors)

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- Bounding the Actual Delay
  - ➤ max actual delay =
    - propagation delay (itself) + max lag time (predecessors)  $\leq$  max propagation delay (predecessors)
  - ➤ Max actual delay cannot be reached for all nodes
- Only the maximum actual delay is insufficient





# 1. NC & DAG 2. New Model **3. LP Attack**

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General case: Concrete attack strategy



Results and security analysis



Consider two group of blocks:



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  - large and many, such as transaction blocks

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 $\delta_{max}^* > \delta_{max}^+$ 



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- Adversary's target
  - $\succ$  average actual delay of  $B^+$ 
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- Adversary's target
  - > average actual delay of  $B^+$ 
    - the average delay of a block accepted by every node
    - reflects the wasted computing power
- Since block mining process is random and unpredictable, adversary maximizes the expectation.







Maximize the "damage" of one potential LP

# Propagating one potential Late-predecessor



## Maximize the "damage" of one potential LP

given  $B^*$  (mined earlier) and  $B^+$ 

- ≻ the probability of  $B^* \leftarrow B^+$
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Optimal strategy:

> some nodes ( $\rho$ %) receive  $B^*$  before  $B^+$  is mined

> other nodes receive  $B^*$  at the maximum propagation delay

# Propagating one potential Late-predecessor





# Consider a sequence of potential $B^*$



maximize the probability of LP appearing: each node has a potential B\*

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#### 19

# Consider a sequence of potential $B^*$

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- > increase lag time: shorten the interval to obtain  $B^*$
- increase number of affected nodes: reduce group size





trade-off

#### 19

# Consider a sequence of potential $B^*$

**G**₁

 $\mathbf{G}_{2}$ 

G<sub>3</sub>

- maximize the probability of LP appearing: each node has a potential B\*
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predecessor successor
arrival time
time
time
potential LP

trade-off

#### Attack Results



#### Optimal *s*

TABLE I: The optimal s that maximizes  $\mathbb{E}[\Delta^+]$ , where k is the expected number of in-propagation blocks in  $\mathcal{B}^*$  in a round.

k	(0.5,2.53)	[2.54,9.81)	[9.82,18.64)	[18.65,20]
s	2	3	4	5

Computing the result

$$\mathbb{E}[\overline{\Delta}^+] = \delta_{\max}^+ + (1 - 1/s)(k - s(1 - \omega))f^*$$

$$k = f^* \cdot (\delta_{\max}^* - \delta_{\max}^+) \qquad \omega = (1 - f^*/s)^{\delta_{\max}^* - \delta_{\max}^+}$$

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longer actual delays

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Ionger propagation delay of LP

higher generation rate of LP



- As nodes have different delays for the same late predecessor, we cannot replace the delay in existing UDBM analyses.
- Chain growth
  - using average actual delay to compute discounted computing power
- Chain quality
  - comparing the discounted chain growth with the adversary's computing power
- Common prefix
  - probability of splitting nodes to work on two distinct chains with different block delays

# Security Properties in the Presence of an LP Attacker

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higher average actual delay leads to lower security level



# **1. NC & DAG**

2. New Model

# 3. LP Attack 4. Examples & Simulation

Prism's security-performance trade-off

#### ➡ OHIE's security-performance trade-off



Simulation of Prism and OHIE

# Prism's security-performance trade-off



Original paper of Prism claims that

changing the parameters of transaction blocks (size and rate) doesn't affect the security



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# Prism's security-performance trade-off

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#### Apply our analyses to Prism

- > delay of proposer blocks is related to tx block's
  - propagation delay

i.e. Throughput

• generation rate



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Security-performance trade-off in Prism still exists
 > throughput ↑ security ↓ latency ↑



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# OHIE's security-performance trade-off



- OHIE's performance relies on the short and stable block propagation delay.
  - More than 50% of the network capacity propagation delay increases



# OHIE's security-performance trade-off

 $\succ$  More than 50% of the network capacity

 $\rightarrow$  propagation delay increases

> actual delay of all blocks increases

propagation delay.

Apply our analyses to OHIE

OHIE's performance relies on the short and stable block





# OHIE's security-performance trade-off



OHIE's performance relies on the short and stable block propagation delay.

- More than 50% of the network capacity propagation delay increases
- Apply our analyses to OHIE
   > actual delay of all blocks increases
- Security is lower when increasing throughput of OHIE by
  - increasing the block size
  - increasing the number of parallel chains (more frequent trailing blocks)



Simulation

We modify SimBlock by adding 1000 LoC to evaluate Prism's and OHIE

#### Results



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#### Results (Prism as an example)

- > our theoretical analysis is precise
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#### Results (Prism as an example)

- > our theoretical analysis is precise
  - original paper is 0.48, simulation is 0.39
- > UDBM downgrades the security
  - UBDM is 0.27
- Existing DAG-based protocols still have not overcome the trade-off between security and performance



# 5 Conclusion & Future works



#### Our works:

- identified vulnerabilities in previous works
- ➡ proposed a new model called CBM
- ➡ presented a sound attack strategy
- exemplified analysis on Prism and OHIE.

## 5 Conclusion & Future works

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### → Future works:

- **?** Generalizability of CBM
- **?** Practicality and Optimality of Our Attack
- **?** Generalizability of the Tradeoff
- ? Improving DAG-based Protocols





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