# Bobtail: Improved Blockchain Security With Low-Variance Mining 

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## Compressed Review of Blockchains



- Ledger comprises set of transactions
- Financial, logistical, legal, ...
- PoW: not the only approach, but most popular and relatively easy to analyze



## Proof-of-Work Mining Basics

- Miners repeatedly hash block header
- Hashes are within $[0, S]$
- A block is mined when hash falls below $t$
- Block time $T$ is function of hash rate $h$ (seconds)
- Convention is to extend longest chain



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- Game repeats


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## Mining statistics

- Time to draw below threshold is approximately Expon $\left(\frac{T}{q}\right)$
- $20 \%$ miner expects to take 4 times as long to mine a block as others



## Double-spending Attack

- Alice trades car for 1 BTC
- Transaction appears in block 1
- Assumes majority are mining chain
- Alice knows about law of large numbers
- Goods are released only once payment has $z$ "confirmations"



## Double-spending Attack

- Bob steals goods if red chain grows longer than blue
- Relies on high variance of the exponential distribution
, Goods worth more than cost of attack?



## Attack Success Probability

$$
\text { attacker mining power }-0.1-0.2-0.3-0.4-0.45
$$

- Attacker needs to get ahead by at least one block
sometime after the first $z$ blocks
- Even a 20\% miner has 5\% chance of winning after 6 blocks



## Bobtail Protocol Details

- Assemble a block containing transactions
- Hash header as usual to generate "proofs"
- Disseminate proofs that are "low enough" to neighbors
- Maintain queue of lowest $k$ proofs
- Assemble $k$ proofs whose mean is below $t$
, Each proof miner receives reward



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- Each draw still "costs" a hash
- First 2 to cross threshold win
- Winners receive a reward and lowest proposes a block



## Impact on Doublespend Attack Efficacy

$$
\text { attacker mining power }-0.1-0.2-0.3-0.4-0.45
$$

- Status quo (Bitcoin)
- 20\% attacker succeeds approximately $5 \%$ of the time after 6 confirmations
- Bobtail with $\mathrm{k}=20$
- $20 \%$ attacker succeeds less than $1 \%$ of the time with just 2 confirmations


## Relative Statistics

- Mining time with Bobtail for fixed target $t$ :
- Expected value increases by $\frac{k+1}{2}$
- Variance increases by $\frac{(k+1)(2 k+1)}{6 k}$
- When expected times are aligned:
, $t_{k}=\frac{k+1}{2} t$
- Relative variance $O(1 / k)$



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- Size of meta data increases by $k \cdot 160 \mathrm{~B}$
- Increased network overhead
- Mitigated by not sending proofs in the "tail"

Gamma shape $k$


- Graphene can be used to reduce redundancy


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- Size of meta data increases by $k \cdot 160 \mathrm{~B}$
- Increased network overhead
- New attacks must be considered
- Proof withholding
- Denial-of-Service (DoS)


## Summary

- Mining process is akin to a lottery
- We can skew statistics in favor of honest majority
- This greatly mitigates fundamental attacks
- Doublespend susceptibility reduced by orders of magnitude
- Primary cost is increased network and block overhead

